

For each of the situations below:

- Think about what is happening to the ice/water/steam.
- Decide which equation makes the most sense to use → write the original equation!
- Identify what each of the numbers means.
- Plug in numbers with units and solve, answer with the correct number of sig figs.

1. How much energy is required to raise 125 g of liquid water from 20.°C to 100.°C?

$$m = 125g \quad Q = mc\Delta T$$

$$\Delta T = 100^\circ\text{C} - 20^\circ\text{C} = 80^\circ\text{C}$$

$$Q = ? \quad Q = 125g \times 1.0 \frac{\text{cal}}{g^\circ\text{C}} \times 80^\circ\text{C} = \boxed{10000 \text{ cal}}$$

or $1.0 \times 10^4 \text{ cal}$

2. Once that liquid water (from #1) is at 100.°C, how much energy is required to vaporize all of it?

$$Q = mH_v \quad Q = 125g \times 539.4 \frac{\text{cal}}{g}$$

$$Q = ? \quad Q = 67425 \text{ cal} = \boxed{67400 \text{ cal}}$$

$$H_v = 539.4 \frac{\text{cal}}{g}$$

3. If you add 3750. cal of energy to solid ice at 0.0°C, how many grams (mass) of ice can be melted?

$$Q = mH_f \quad 3750. \text{ cal} = m \times 79.72 \frac{\text{cal}}{g}$$

$$Q = 3750. \text{ cal} \quad m = 47.0396g = \boxed{47.04g}$$

$$m = ?$$

4. Once the ice in #3 is melted (at 0.0°C), if you add another 3750. cal of energy to it, what temperature will the liquid water be?

$$Q = mc\Delta T \quad 3750. \text{ cal} = 47.04g \times 1 \frac{\text{cal}}{g^\circ\text{C}} \times \Delta T \quad \Delta T = T_f - T_i$$

$$Q = 3750 \text{ cal} \quad 79.72^\circ\text{C} = T_f - 0.0^\circ\text{C}$$

$$m = 47.04g \quad \Delta T = 79.72^\circ\text{C} \quad \boxed{T_f = 79.72^\circ\text{C}}$$

$$\Delta T = ?$$

5. How many calories are needed to raise 38 g of liquid water by 40.°C?

$$Q = ? \quad Q = mc\Delta T$$

$$m = 38g \quad Q = 38g \times 1 \frac{\text{cal}}{g^\circ\text{C}} \times 40^\circ\text{C} \quad Q = 1520 \text{ cal} = \boxed{1500 \text{ cal}}$$

$$\Delta T = 40^\circ\text{C}$$

6. If you add 4500 cal of energy to liquid water that is already at 100.°C, how many grams of water can be vaporized?

$$Q = mH_v \quad 4500 \text{ cal} = m \times 539.4 \frac{\text{cal}}{g}$$

$$Q = 4500 \text{ cal} \quad m = 8.3426g = \boxed{8.3g}$$

$$m = ?$$

7. How much energy does it take to melt 1 g of ice at 0°C? How much energy does it take to vaporize 1 g of water at 100°C? What is the name of each of those constants (the number you just found)?

melt: $79.72 \frac{\text{cal}}{g} \rightarrow$ heat of fusion vaporize: $539.4 \frac{\text{cal}}{g} \rightarrow$ heat of vaporization

8. Propose one reason why the two numbers in #7 are so different from one another. (hint: think about why one phase change might take more energy)

It takes much more energy to vaporize 1 g of a material (pull the particles completely apart from one another) than to melt 1 g of a material (let the particles slide past one another).

9. If you remove 3200 cal from 58 g of liquid water, how much will the temperature decrease?

$$Q = 3200 \text{ cal} \quad Q = mc\Delta T \quad \Delta T = 55.17^\circ\text{C}$$

$$m = 58g \quad 3200 \text{ cal} = 58g \times 1 \frac{\text{cal}}{g^\circ\text{C}} \times \Delta T \quad \Delta T = -55^\circ\text{C} \text{ (a decrease)}$$

10. If the water in #9 started at 95°C, what temperature will it end at?

$$\Delta T = T_f - T_i \quad -55^\circ\text{C} = T_f - 95^\circ\text{C}$$

$$T_f = 40^\circ\text{C}$$

11. How much energy needs to be removed to condense (the opposite of vaporize) 85 g of water vapor at 100.°C?

$$m = 85\text{g}$$

$$Q = ?$$

$$H_c = -539.4 \frac{\text{cal}}{\text{g}}$$

$$Q = m H_c$$

$$Q = 85\text{g} \times -539.4 \frac{\text{cal}}{\text{g}}$$

$$Q = -45849 \text{ cal}$$

$$= -46000 \text{ cal}$$

↑ removed

12. How much energy needs to be removed to freeze (the opposite of melt) 85 g of liquid water at 0.0°C?

$$Q = m H_s$$

$$Q = 85\text{g} \times -79.72 \frac{\text{cal}}{\text{g}}$$

$$Q = -6776.2 \text{ cal} = -6800 \text{ cal}$$

↑ removed

13. How much energy needs to be removed to cool 46 g of liquid water from 75°C to 25°C?

$$Q = m c \Delta T$$

$$m = 46\text{g}$$

$$\Delta T = -50^\circ\text{C}$$

$$Q = 46\text{g} \times 1 \frac{\text{cal}}{\text{g}^\circ\text{C}} \times -50^\circ\text{C}$$

$$Q = -2300 \text{ cal}$$

14. If you have 57 g of solid ice at 0.0°C and you want to melt all of it, raise it all to 100.°C, and then vaporize all of it, how much energy must you add? (hint: think about what is happening to the ice/water/steam)

$$Q = m H_f = 57\text{g} \times 79.72 \frac{\text{cal}}{\text{g}} = 4544.04 \text{ cal}$$

$$Q = m c \Delta T = 57\text{g} \times 1 \frac{\text{cal}}{\text{g}^\circ\text{C}} \times 100^\circ\text{C} = 5700 \text{ cal}$$

$$Q = m H_v = 57\text{g} \times 539.4 \frac{\text{cal}}{\text{g}} = 30745.8 \text{ cal}$$

$$= 40989.84 \text{ cal}$$

$$= 41000 \text{ cal}$$

15. If you have 28 g of water vapor at 100.°C and you want to condense all of it, cool it all to 0.0°C, and freeze all of it, how much energy must be removed? (hint: think about what is happening to the ice/water/steam)

$$Q = m H_c = 28\text{g} \times -539.4 \frac{\text{cal}}{\text{g}} = -15103.2 \text{ cal}$$

$$Q = m c \Delta T = 28\text{g} \times 1 \frac{\text{cal}}{\text{g}^\circ\text{C}} \times -100^\circ\text{C} = -2800 \text{ cal}$$

$$Q = m H_s = 28\text{g} \times -79.72 \frac{\text{cal}}{\text{g}} = -2232.16 \text{ cal}$$

$$= -20135.36 \text{ cal}$$

$$= -20000 \text{ cal}$$

16. Find the Physical Constants for Water in your data book. There is a different "c" value (specific heat capacity) for solid water (ice). What is that value? If you have 15 g of solid ice at -14°C and you want to raise the temperature to 0.0°C how much energy will you have to add?

$$Q = m c \Delta T$$

$$m = 15\text{g}$$

$$c = 0.502 \frac{\text{cal}}{\text{g}^\circ\text{C}}$$

$$\Delta T = 14^\circ\text{C}$$

$$Q = 15\text{g} \times 0.502 \frac{\text{cal}}{\text{g}^\circ\text{C}} \times 14^\circ\text{C}$$

$$Q = 105.42 \text{ cal} = 110 \text{ cal}$$

17. Challenge ☺: You have 43 g of solid ice at 0.0°C. You add 4300 cal of energy to it. Describe the status of the ice/water/steam at the end. Is it all the same state? What state is that? What temperature is it?

$$Q = m H_f = 43\text{g} \times 79.72 \frac{\text{cal}}{\text{g}} = 3427.96 \text{ cal}$$

needed to melt all the ice

$$4300 - 3427.96 = 872.04 \text{ cal}$$

left to add after it has melted

$$Q = m c \Delta T \quad 872.04 \text{ cal} = 43\text{g} \times 1 \frac{\text{cal}}{\text{g}^\circ\text{C}} \times \Delta T$$

$\Delta T = 20.28^\circ\text{C}$
 \times started at 0°C so final is $20.^\circ\text{C}$